# CURRICULUM AND SYLLABUS FOR M.Sc. (Mathematics) - MASTER OF SCIENCE (TWO YEARS - FULL TIME) REGULATION - 2018

(Applicable to the students admitted from the academic year 2018-2019 onwards)

| Semester | Course | Course Name                          | Lecture | Tutorial | Practical | Credit |
|----------|--------|--------------------------------------|---------|----------|-----------|--------|
|          | Code   |                                      |         |          |           |        |
|          | YMA101 | Groups and Rings                     | 4       | 1        | 0         | 5      |
|          | YMA102 | Analysis - I                         | 4       | 1        | 0         | 5      |
| I        | YMA103 | Differential Equations               | 3       | 1        | 0         | 4      |
|          | YMA104 | Discrete Mathematics                 | 3       | 1        | 0         | 4      |
|          | YMA1E* | One among the list of Electives (1E) | 3       | 0        | 0         | 3      |
|          |        |                                      |         |          |           | 21     |

# \* List of Electives (1E)

| <b>Elective Code</b> | Course Name        | L | T | P | С |
|----------------------|--------------------|---|---|---|---|
| 01                   | Graph Theory       | 3 | 0 | 0 | 3 |
| 02                   | Coding Theory      | 3 | 0 | 0 | 3 |
| 03                   | Mathematical Logic | 3 | 0 | 0 | 3 |

| Semester | Course | Course Name                           | Lecture | Tutorial | Practical | Credit |
|----------|--------|---------------------------------------|---------|----------|-----------|--------|
|          | Code   |                                       |         |          |           |        |
|          | YMA201 | Linear Algebra                        | 4       | 1        | 0         | 5      |
|          | YMA202 | Analysis - II                         | 4       | 1        | 0         | 5      |
|          | YMA203 | Differential Geometry                 | 3       | 1        | 0         | 4      |
| II       | YMA204 | Operations Research                   | 3       | 1        | 0         | 4      |
|          | YMA2E* | One among the list of Electives (2 E) | 3       | 0        | 0         | 3      |
|          |        |                                       |         |          |           | 21     |

# \* List of Electives (2E)

| <b>Elective Code</b> | Course Name                    | L | T | P | C |
|----------------------|--------------------------------|---|---|---|---|
| 01                   | Algebraic Number Theory        | 3 | 0 | 0 | 3 |
| 02                   | Data structures and Algorithms | 3 | 0 | 0 | 3 |
| 03                   | Fuzzy sets and Fuzzy logic     | 3 | 0 | 0 | 3 |

| Semester | Course<br>Code | Course Name                           | Lecture | Tutorial | Practical | Credit |
|----------|----------------|---------------------------------------|---------|----------|-----------|--------|
|          | YMA301         | Field Theory                          | 3       | 1        | 0         | 4      |
|          | YMA302         | Topology                              | 4       | 1        | 0         | 5      |
|          | YMA303         | Measure Theory                        | 3       | 1        | 0         | 4      |
| III      | YMA304         | Mathematical Statistics               | 3       | 1        | 0         | 4      |
|          | YMA3E*         | One among the list of Electives (3 E) | 3       | 0        | 0         | 3      |
|          |                |                                       |         |          |           | 20     |

# \* List of Electives (3E)

| <b>Elective Code</b> | Course Name              | L | T | P | С |
|----------------------|--------------------------|---|---|---|---|
| 01                   | Analytical Number Theory | 4 | 0 | 0 | 4 |
| 02                   | Numerical Methods        | 4 | 0 | 0 | 4 |
| 03                   | Commutative Algebra      | 4 | 0 | 0 | 4 |

| Semester | Course<br>Code | Course Name          | Lecture | Tutorial | Practical | Credit |
|----------|----------------|----------------------|---------|----------|-----------|--------|
|          | YMA401         | Complex Analysis     | 4       | 1        | 0         | 5      |
|          | YMA402         | Functional Analysis  | 4       | 1        | 0         | 5      |
| IV       | YMA403         | Stochastic Processes | 3       | 1        | 0         | 4      |
|          |                | Project work         |         |          |           | 8      |
|          |                |                      |         |          |           | 22     |

**Total Number of Credits** : 84

| CO                                    | URSE     | CODE       | COURSE NAME                                                                    | L         | Т      | P                | C        |
|---------------------------------------|----------|------------|--------------------------------------------------------------------------------|-----------|--------|------------------|----------|
|                                       | YMA1     | 01         | GROUPS AND RINGS                                                               | 4         | 1      | 0                | 5        |
| С                                     | P        | A          |                                                                                |           |        |                  |          |
| C                                     | 1        | A          |                                                                                |           |        |                  |          |
| 5                                     | 0        | 0          |                                                                                | L         | Т      | Р                | Н        |
|                                       | <u>i</u> |            |                                                                                | 4         | 1      | 0                | 5        |
| PRE                                   | REQUI    | SITE: B    | asic concepts of sets, groups and rings                                        |           | .1     |                  |          |
| COU                                   | RSE OU   | JTCOME     | S:                                                                             |           |        |                  |          |
| Cour                                  | se outco | mes:       |                                                                                | Doma      | in     | Level            |          |
| CO1                                   |          | _          | plain Subgroups, Normal subgroups and Quotient ge's Theorem.                   | Cognit    | tive   | Remem<br>Underst |          |
| CO2                                   | : Define | and Exp    | plain Homomorphism Theorems, Isomorphism                                       | Cognit    | tive   | Remem            | _        |
|                                       |          |            | omorphisms Theorems, Cayley's theorem.                                         |           |        | Underst          | anding   |
|                                       | Permu    | tation gro | oups, Another Counting principle.                                              |           |        |                  |          |
| CO3                                   | : Define | and Ex     | plain Sylow's Theorems and their simple                                        | Cognit    | tive   | Remem            |          |
|                                       | applica  | tions, Di  | rect Products: External and Internal, Finite                                   |           |        | Underst          | anding   |
|                                       | Abelia   | n Groups   | •                                                                              |           |        |                  |          |
| CO4                                   | : Define | and Ex     | plain Rings, Subrings, Ideals, Factor Rings,                                   | Cognit    | tive   | Rememberin       |          |
|                                       | Homo     | morphism   | and Integral Domains. Maximal and prime                                        |           |        | Underst          | anding   |
|                                       |          |            | of Quotients of an integral domain.                                            |           |        |                  |          |
| CO <sub>5</sub>                       |          |            | lain Euclidean Ring, A Particular Euclidean                                    | Cognit    | tive   | Remem            |          |
|                                       |          |            | al Ring, and Polynomial over the Rational Field,                               |           |        | Underst          | anding   |
| <b>T 13 17</b> 7                      |          | mial Ring  | gs over Commutative Rings.                                                     |           |        |                  | 1.5      |
| UNIT                                  |          | 1          | or Caronia Culturana Namalantana and One                                       | 4:4 C     |        | T                | 15       |
| Theo                                  |          | example    | s: Groups, Subgroups, Normal subgroups and Quo                                 | neni Gr   | oups,  | Lagran           | ge s     |
| UNIT                                  |          |            |                                                                                |           |        |                  | 15       |
|                                       |          | ism Theo   | orems, Isomorphism Theorems, Automorphisms                                     | Theore    | ems.   | Cavley'          |          |
|                                       |          |            | groups, Another Counting principle.                                            | 1110010   | ,      | cujicj           |          |
| UNIT                                  |          |            |                                                                                |           |        |                  | 15       |
|                                       |          |            | nd their simple applications, Direct Products: E                               | xternal   | and    | Internal,        | Finite   |
|                                       | ian Grou | ıps.       |                                                                                |           |        |                  | 1 1 -    |
| UNIT                                  |          | aga Idaal  | G. Footor Bings, Homomorphism, Integral Domain                                 | a Mayi    | mal a  | nd nrim          | 15       |
| _                                     |          | _          | s, Factor Rings, Homomorphism, Integral Domain notients of an integral domain. | s. iviaxi | mai a  | на рип           | Ē.       |
| UNIT                                  |          | 210 01 Qt  | otento of an integral domain.                                                  |           |        |                  | 15       |
|                                       |          | ng, A Pa   | rticular Euclidean Ring, Polynomial Ring, Polynor                              | nial ove  | er the | Rationa          | <u>1</u> |
|                                       |          |            | r Commutative Rings.                                                           |           |        |                  |          |
| · · · · · · · · · · · · · · · · · · · | ECTURE   |            | ORIAL                                                                          |           |        | <b>TO</b> 7      | ΓAL      |
| 60                                    |          | 15         |                                                                                |           |        | 75               |          |
| 1EX                                   | TBOOK    |            |                                                                                |           |        |                  |          |

1. Herstein, I.N., "Topics in Algebra", Willey Eastern 1975.

Unit I - Chapter 2 (Section 2.1 - 2.6)

Unit II - Chapter 2 (Section 2.7 - 2.11)

Unit III - Chapter 2 (Section 2.12 - 2.14)

Unit IV - Chapter 3 (Section 3.1 - 3.6)

Unit V - Chapter 3 (Section 3.7 - 3.11)

#### **REFERENCES**

**COURSE CODE** 

UNIT II

Basic Topology:

1. John B. Fraleigh, "A First Course in Abstract Algebra", Narosa Publication, Third Edition, 2003.

**COURSE NAME** 

L

 $\mathbf{T}$ 

P

 $\mathbf{C}$ 

15

2. Cohn P. M., "Basic Algebra", Springer's Publications, Second Edition, 2005.

|      | YMA102 ANALYSIS - I |           | 4                                                                                                       | 1        | 0     | 5     |                     |
|------|---------------------|-----------|---------------------------------------------------------------------------------------------------------|----------|-------|-------|---------------------|
| C    | P                   | A         |                                                                                                         |          |       |       |                     |
| 5    | 0                   | 0         |                                                                                                         | L        | T     | P     | H                   |
|      |                     |           |                                                                                                         | 4        | 1     | 0     | 5                   |
| PRE  | REQU                | ISITE:    |                                                                                                         | <u> </u> |       |       | <u> </u>            |
| COL  | J <b>RSE (</b>      | OUTCO     | MES: Basic concepts of real numbers                                                                     |          |       |       |                     |
| Cou  | rse out             | comes:    |                                                                                                         | Doma     | ain   | Level |                     |
| CO1  | : Defin             | e and E   | xplain the Real and Complex Number Systems.                                                             | Cogn     | itive |       | nbering<br>tanding  |
| CO2  | : Defin             | e and E   | xplain Basic Topology.                                                                                  | Cogn     | itive |       | nbering<br>tanding  |
| CO3  | : Defin             | e and E   | xplain convergence of sequences and series                                                              | Cogn     | itive |       | nbering<br>tanding  |
| CO4  | : Defin             | e and E   | xplain Continuity of functions                                                                          | Cogn     | itive |       | nbering<br>tanding  |
|      | inuity o            |           | <b>Explain</b> the derivative of a real function, the atives, Derivatives of Higher Order, and Taylor's | Cogn     | itive |       | nbering<br>standing |
| UNI  | T I The             | Real a    | nd Complex Number Systems:                                                                              |          |       |       | 15                  |
| Orde | red sets            | s, The re | al field, The complex field, Euclidean spaces.                                                          |          |       |       |                     |

| Finite, Countable and Uncountable sets, Metric space, Compact sets, Perfect Sets, Connected |         |
|---------------------------------------------------------------------------------------------|---------|
| Sets.                                                                                       |         |
| UNIT III Numerical Sequences and Series:                                                    | 15      |
| Convergent sequences (in Metric Spaces), subsequences, Cauchy sequences, Upper and          | Lower   |
| Limits, Some Special Sequences, Series, Series of Negative terms, The root and ratio tests. |         |
| UNIT IV Continuity:                                                                         | 15      |
| Limits of functions (in metric spaces) Continuous functions, Continuity and                 |         |
| Compactness, Continuity and Connectedness, Discontinuities, Monotonic functions, Uniform    |         |
| Continuity, Infinite Limits and Limits at Infinity.                                         |         |
| UNIT V Differentiation:                                                                     | 15      |
| The Derivative of a Real Function, Mean Value Theorems, The Continuity of Derivative        | atives, |
| L'Hospital's Rule, Derivatives of Higher Order, Taylor's Theorem.                           |         |
| LECTURE TUTORIAL TOTA                                                                       | L       |
| 60 15 75                                                                                    |         |
| TEXTBOOK                                                                                    |         |

1. Walter Rudin,"Principles of Mathematical Analysis", (3rd Edition) McGraw-Hill, 2016.

Unit I - Chapter 1 (Pages: 3-5, 8-11, 12-16)

Unit II - Chapter 2 (Pages: 24 - 42)

Unit III - Chapter 3 (Pages: 47-63, 65-69)

Unit IV - Chapter 4 (Pages: 83-97) Unit V - Chapter 5 (Section 103-111)

- 1. Shanti Narayan,"A Course of Mathematical Analysis", S.Chand & Co, 2005.
- 2. Apostol, T.M,"Mathematical Analysis", 2<sup>nd</sup> Edition,1996.
- 3. Malik, S.C,"Mathematical Analysis", Wiley Eastern Ltd, 2017.

| CO     | OURSE CODE COURSE NAME |            | L                            | Т | P        | C     |   |
|--------|------------------------|------------|------------------------------|---|----------|-------|---|
| YMA103 |                        | 03         | DIFFERENTIAL EQUATIONS       | 3 | 1        | 0     | 4 |
| С      | P                      | A          |                              |   |          |       |   |
| 4      | 0                      | 0          |                              | L | T        | P     | Н |
|        | <u> </u>               |            |                              | 3 | 1        | 0     | 4 |
| PRE    | REQU                   | ISITE: Dif | ferentiation and Integration |   | <u> </u> |       |   |
| COU    | IRSE O                 | UTCOMES    | :                            |   |          |       |   |
| Cour   | Course outcomes:       |            |                              |   | in       | Level |   |

| <b>CO1:</b> Find The general solution of the homogeneous equations using various methods.         | Cognitive | Remembering Understanding |
|---------------------------------------------------------------------------------------------------|-----------|---------------------------|
| <b>CO2: Solve</b> the homogeneous linear system with constant coefficients and special functions. | Cognitive | Applying                  |
| CO3: Find the critical points and stability for linear systems by Liapounov's direct method.      | Cognitive | Remembering Understanding |
| <b>CO4:</b> Solve First order linear partial differential equations using various methods.        | Cognitive | Applying                  |
| CO5: Solve initial and boundary value problems.                                                   | Cognitive | Applying                  |
| UNIT I                                                                                            | <u> </u>  | 12                        |

The general solution of the homogeneous equation – The use of one known solution to find another – The method of variation of parameter – Power series solutions – Series solutions of first order equations – Second order linear equations – ordinary points – Regular singular points – Gauss hyper geometric equations – the point 0 at infinity.

UNIT II

Legendre polynomials – Properties of Legendre polynomials – Bessel functions – The gamma function – Properties of Bessel function – linear systems – Homogeneous linear system with constant coefficients.

UNIT III

12

The existence and uniqueness of solutions – The method of Successive approximation – Picard's theorem – Types of critical points – Critical points and stability for linear systems – Stability by Liapunov's direct method.

UNIT IV 12

First order partial differential equations – Linear equations of the first order – Partial differential equations – Compatible systems – Charpit's method – Jacobi's method – Integral surface through a given circle.

UNIT V 12

Solution of initial and boundary value problems – Characteristics – D'Alembert's solution – Significance of characteristic curves – Laplace transforms solutions for displacement in a string – a long string under its weight – Longitudinal vibration of a elastic bar with prescribed force on one end – free vibrations of string.

| LECTURE | TUTORIAL | TOTAL |
|---------|----------|-------|
| 45      | 15       | 60    |

#### **TEXTBOOK**

- 1. Simmons, G.F.,"Differential Equations with Applications and Historical Notes", TMH, New Delhi, 2003
- 2. T. Amarnath, "An Elementary Course in Partial Differential Equations", Narosa, New Delhi, 1997.
  - Unit I- Chapter 3: Sections 15,16,19, Chapter 5: Sections 26 to 31
  - Unit II- Chapter 8: Sections 44 to 47, Chapter 10: Sections 54 to 56
  - Unit III- Chapter 13: Sections 68, 69, Chapter 11: Sections 60, 61
  - Unit IV Chapter 1: Sections 1.4 to 1.9
  - Unit V Chapter 2: Sections 2.1, 2.2, 2.3.1, 2.3.2, 2.3.3, 2.3.5, 2.5.1, 2.5.2

- 1. W.T.Reid, "Ordinary Differential Equations", John Wiley, New York, 1971.
- 2. E.A.Coddington and E.Levinson, "Theory of ODE", Mc Graw Hill Publishing Company, New york, 1955 .
- 3. J.N. Sneddon, "Elements of Partial Differential Equations", Mc Graw Hill Publishing Company, New york, 1957.

| COURSE CODE     |           | ODE      | COURSE NAME                                           | L          | T      | P                 | С        |  |
|-----------------|-----------|----------|-------------------------------------------------------|------------|--------|-------------------|----------|--|
| YMA104          |           | 4        | DISCRETE MATHEMATICS                                  | 3          | 1      | 0                 | 4        |  |
| С               | P         | A        |                                                       |            |        |                   |          |  |
|                 |           |          |                                                       |            |        |                   |          |  |
| 4               | 0         | 0        |                                                       | L          | Т      | P                 | H        |  |
|                 | i         | <u>i</u> |                                                       | 3          | 1      | 0                 | 4        |  |
| PRE             | REQUI     | SITE:    | Algebra                                               |            |        |                   |          |  |
| COL             | IRSE OU   | JTCON    | IES:                                                  |            |        |                   |          |  |
| Cou             | rse outco | mes:     |                                                       | Doma       | in     | Level             |          |  |
| CO <sub>1</sub> | : Defin   | e and ]  | Explain Basic logical operations.                     | Cogni      | tive   | Rememl<br>Underst |          |  |
| CO2             |           |          | Explain the theory of inference for the statement     | Cogni      | tive   | Remem             |          |  |
|                 | Calcu     | lus.     |                                                       |            |        | Unders            | anding   |  |
| CO3             | 3: Solve  | Recurr   | ence Relations using Generating Functions.            | Cogni      | tive   | Applyin           | ing      |  |
| CO <sub>4</sub> | l: Define | and E    | Explain Lattices and Boolean Algebra.                 | Cogni      | tive   | Rememl            |          |  |
| COS             | 5: Defin  | e and l  | E <b>xplain</b> Grammar and Languages.                | Cogni      | tive   | Remem             | <u> </u> |  |
|                 |           |          |                                                       |            |        | Underst           | anding   |  |
|                 |           |          | ical Logic :                                          |            |        |                   | 12       |  |
|                 | _         | -        | ions, conditional and biconditional statements, tauto | ologies, c | ontra  | diction,          |          |  |
|                 | nal form  |          |                                                       |            |        |                   | T        |  |
|                 |           |          | y of inference for the statement Calculus:            |            |        |                   | 12       |  |
|                 |           |          | Consistency, Automatic Theorem proving, Predicate     | e Calculu  | ıs, qu | antifiers,        |          |  |
| Infer           | ence Th   | eory of  | the Predicate Calculus.                               |            |        |                   |          |  |
|                 |           |          | nce Relations and Generating Functions:               |            |        |                   | 12       |  |
| -               |           | _        | ions, telescopic form, recursion theorem, closed for  | m expres   | sion,  | generati          | ng       |  |
|                 |           |          | f recurrence relation using generating function.      |            |        |                   |          |  |
|                 |           |          | and Boolean Algebra:                                  | D 1        |        | 1                 | 12       |  |
| Parti           | al ordere | ed sets, | Properties of Lattices, Lattices as Algebraic System  | ns, Boole  | an A   | gebra.            |          |  |
| UNI             | ΓV Gr     | ammai    | and Languages:                                        |            |        |                   | 12       |  |

Phrase structure grammars, rewriting rules, derivation sentential forms, language generated by grammar, regular, context free and context sensitive grammar and languages.

| LECTURE | TUTORIAL | TOTAL |
|---------|----------|-------|
| 45      | 15       | 60    |

### TEXTBOOK

- 1. P. Tremblay, R. Manohar,"Discrete Mathematical Structure with Applications to Computer Science", Mc Graw-Hill International Edition, 1997.
  - Unit I Chapter 1 (Section 1.1,1.2 & 1.3)
  - Unit II Chapter 1 (Section 1.4, 1.5 & 1.6)
  - Unit IV Chapter 4 (Section 4.1& 4.2)
  - Unit V Chapter 4 (Section 4.6)
- 2. Alan Doerr, "Applied Discrete Structure for Computer Science", Pearson Education, 2013 Unit III – Chapter 8 (Section 8.1,8.2,8.3 &8.5)

## REFERENCE

1. Kenneth H. Rosen, "Discrete Mathematics and Its Applications", Mc Graw-Hill International Edition, 2002.

| COURSE CODE |       |    | COURSE NAME  | L | T | P | C |
|-------------|-------|----|--------------|---|---|---|---|
|             | YMA10 | 15 | GRAPH THEORY | 3 | U | 0 | 3 |
| С           | P     | A  |              |   |   |   |   |
| 3           | 0     | 0  |              | L | Т | P | Н |
|             |       |    |              | 3 | 0 | 0 | 3 |

## PREREQUISITE:

| <b>COURSE OUTCOMES:</b> Basic concepts of Graph Theory                                                                  |           |                           |
|-------------------------------------------------------------------------------------------------------------------------|-----------|---------------------------|
| Course outcomes:                                                                                                        | Domain    | Level                     |
| CO1: Define and Explain Graphs, subgraphs and trees.                                                                    | Cognitive | Remembering Understanding |
| CO2: Define and Explain Connectivity - Blocks - Euler tours - Hamilton Cycles.                                          | Cognitive | Remembering Understanding |
| <b>CO3: Define and Explain</b> Matchings and Coverings in Bipartite Graphs, Edge Chromatic Number and Vizing's Theorem. | Cognitive | Applying                  |
| CO4: Define and Explain independent sets and cliques, vertex colourings.                                                | Cognitive | Remembering Understanding |

|                                                                                                                                                                                                                          | d Explain Plane and planar Graphs, Dual graphs,                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | Cognitive                                                           | Rememberin             |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------|------------------------|
|                                                                                                                                                                                                                          | rmula, The Five-Colour Theorem and the Four-                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Understan                                                           |                        |
| Colour Co                                                                                                                                                                                                                | njecture- Applications.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                                                                     |                        |
| UNIT I GRAPI                                                                                                                                                                                                             | IS, SUBGRAPHS AND TREES                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                                                                     | 9                      |
| Graphs and simp                                                                                                                                                                                                          | e graphs - Graph Isomorphism - The Incidence and A                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | djacency Mat                                                        | rices -                |
| Subgraphs - Vert                                                                                                                                                                                                         | ex Degrees - Paths and Connection - Cycles - Trees - 0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | Cut Edges an                                                        | d Bonds - Cu           |
| Vertices.                                                                                                                                                                                                                |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                                                                     |                        |
| UNIT II CONN                                                                                                                                                                                                             | ECTIVITY, EULER TOURS AND HAMILTON (                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | CYCLES                                                              | 9                      |
| Connectivity - B                                                                                                                                                                                                         | ocks - Euler tours - Hamilton Cycles – Applications.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                                     |                        |
| UNIT III MAT                                                                                                                                                                                                             | CCHINGS, EDGE COLOURINGS                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |                                                                     | 9                      |
| Matchings - Mat                                                                                                                                                                                                          | chings and Coverings in Bipartite Graphs - Edge Chro                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | matic Number                                                        | ſ -                    |
| Vizing's Theorem                                                                                                                                                                                                         | n- Applications.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                                                                     |                        |
| UNIT IV INDE                                                                                                                                                                                                             | PENDENT SETS AND CLIQUES, VERTEX COL                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | OURINGS                                                             | 9                      |
| Independent sets                                                                                                                                                                                                         | - Ramsey's Theorem - Chromatic Number - Brooks'                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | Гheorem -                                                           |                        |
| Chromatic Polyn                                                                                                                                                                                                          | omials- Applications.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                                     |                        |
| UNIT V PLAN                                                                                                                                                                                                              | AR GRAPHS                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |                                                                     | 9                      |
|                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                                                                     | •                      |
| Plane and planar                                                                                                                                                                                                         | Graphs - Dual graphs - Euler's Formula - The Five-Co                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | olour Theoren                                                       | 1                      |
|                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | olour Theoren                                                       | 1                      |
|                                                                                                                                                                                                                          | Graphs - Dual graphs - Euler's Formula - The Five-Co                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | olour Theoren                                                       | TOTAL                  |
| and the Four-Col LECTURE 45                                                                                                                                                                                              | Graphs - Dual graphs - Euler's Formula - The Five-Co                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | olour Theoren                                                       |                        |
| and the Four-Col LECTURE 45 TEXTBOOK                                                                                                                                                                                     | Graphs - Dual graphs - Euler's Formula - The Five-Coour Conjecture- Applications.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                     | TOTAL<br>45            |
| and the Four-Col LECTURE 45 TEXTBOOK 1. J.A.Bondy and                                                                                                                                                                    | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", M.                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                                     | TOTAL<br>45            |
| and the Four-Col LECTURE 45 TEXTBOOK 1. J.A.Bondy and Unit I - Chapte                                                                                                                                                    | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3)                                                                                                                                                                                                                                                                                                                                                                                           |                                                                     | TOTAL<br>45            |
| and the Four-Col LECTURE 45 TEXTBOOK 1. J.A.Bondy and Unit I - Chapte Unit II - Chapte                                                                                                                                   | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2)                                                                                                                                                                                                                                                                                                                                   |                                                                     | TOTAL<br>45            |
| and the Four-Col LECTURE 45 TEXTBOOK 1. J.A.Bondy and Unit I - Chapte Unit II - Chapte Unit III - Chapte                                                                                                                 | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2)                                                                                                                                                                                                                                                                          | Iacmillan, Loi                                                      | TOTAL<br>45            |
| and the Four-Col  LECTURE  45  TEXTBOOK  1. J.A.Bondy and Unit I - Chapte Unit II - Chapte Unit III - Chapte Unit IV - Chap                                                                                              | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2) eter 7 (Section 7.1 - 7.2); Chapter 8 (Section 8.1 - 8.2,                                                                                                                                                                                                                | Iacmillan, Loi                                                      | TOTAL<br>45            |
| and the Four-Col  LECTURE 45  TEXTBOOK  1. J.A.Bondy and Unit I - Chapte Unit II - Chapte Unit III - Chapte Unit IV - Chapte Unit IV - Chapte Unit V - Chapte                                                            | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2)                                                                                                                                                                                                                                                                          | Iacmillan, Loi                                                      | TOTAL<br>45            |
| and the Four-Col  LECTURE  45  TEXTBOOK  1. J.A.Bondy and Unit I - Chapte Unit II - Chapte Unit III - Chapte Unit IV - Chapte Unit V - Chapte REFERENCES                                                                 | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2) eter 7 (Section 7.1 - 7.2); Chapter 8 (Section 8.1 - 8.2, eter 9 (Section 9.1 - 9.3, 9.6)                                                                                                                                                                                | Iacmillan, Loi                                                      | TOTAL<br>45            |
| and the Four-Col LECTURE 45 TEXTBOOK  1. J.A.Bondy and Unit I - Chapte Unit II - Chapte Unit III - Chapte Unit IV - Chapte Unit V - Chapte REFERENCES  1. Harary, "Grap                                                  | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2) eter 7 (Section 7.1 - 7.2); Chapter 8 (Section 8.1 - 8.2, er 9 (Section 9.1 - 9.3, 9.6)  In Theory" Narosa Publishing House., 2001.                                                                                                                                      | Jacmillan, Loi                                                      | TOTAL 45 and on, 1976. |
| and the Four-Col  LECTURE  45  TEXTBOOK  1. J.A.Bondy and Unit I - Chapte Unit II - Chapte Unit IV - Chapte Unit IV - Chapte Unit V - Chapte REFERENCES  1. Harary, "Grap 2. A. Gibbons, "A                              | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2) eter 7 (Section 7.1 - 7.2); Chapter 8 (Section 8.1 - 8.2) er 9 (Section 9.1 - 9.3, 9.6)  Theory" Narosa Publishing House., 2001. Igorithmic Graph Theory, Cambridge University Press                                                                                     | Iacmillan, Lor<br>, 8.4)                                            | TOTAL 45 and on, 1976. |
| and the Four-Col  LECTURE  45  TEXTBOOK  1. J.A.Bondy and Unit I - Chapte Unit II - Chapte Unit IV - Chapte Unit IV - Chapte Unit V - Chapte Unit V - Chapte A.Gibbons, "A 3.R.J.Wilson and                              | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2) eter 7 (Section 7.1 - 7.2); Chapter 8 (Section 8.1 - 8.2, er 9 (Section 9.1 - 9.3, 9.6)  In Theory" Narosa Publishing House., 2001.                                                                                                                                      | Iacmillan, Lor<br>, 8.4)                                            | TOTAL 45 and on, 1976. |
| and the Four-Col  LECTURE  45  TEXTBOOK  1. J.A.Bondy and Unit I - Chapte Unit III - Chapte Unit IV - Chapte Unit IV - Chapte Unit V - Chapte Unit V - Chapte Unit V - Chapte A.Gibbons, "A 3.R.J.Wilson and York, 1989. | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2) ter 7 (Section 7.1 - 7.2); Chapter 8 (Section 8.1 - 8.2, er 9 (Section 9.1 - 9.3, 9.6)  In Theory" Narosa Publishing House., 2001.  Ilgorithmic Graph Theory, Cambridge University Press J.J. Watkins, "Graphs: An Introductory Approach", John March 1988 (Section 9.1) | (acmillan, Lor<br>(a, 8.4)<br>(b) (a, Cambridge, b) (b) (a) (a) (a) | 1989. Sons, New        |
| and the Four-Col LECTURE 45 TEXTBOOK  1. J.A.Bondy and Unit I - Chapte Unit II - Chapte Unit IV - Chapte Unit IV - Chapte Unit V - Chapte Unit V - Chapte A.Gibbons, "A 3.R.J.Wilson and York, 1989. 4.V.K. Balakrish    | Graphs - Dual graphs - Euler's Formula - The Five-Cour Conjecture- Applications.  U.S.R. Murthy, "Graph Theory and Applications", Mer 1 (Section 1.1 - 1.7); Chapter 2 (Section 2.1 - 2.3) er 3 (Section 3.1 - 3.2); Chapter 4 (Section 4.1 - 4.2) ter 5 (Section 5.1 - 5.2); Chapter 6 (Section 6.1 - 6.2) eter 7 (Section 7.1 - 7.2); Chapter 8 (Section 8.1 - 8.2) er 9 (Section 9.1 - 9.3, 9.6)  Theory" Narosa Publishing House., 2001. Igorithmic Graph Theory, Cambridge University Press                                                                                     | (acmillan, Lor<br>(a, 8.4)<br>(b) (a, Cambridge, b) (b) (a) (a) (a) | 1989. Sons, New        |

5.S.A.Choudum, "A First Course in Graph Theory", MacMillan India Ltd. 1987.

| COURSE CODE      |                   |                      | COURSE NAME                                                                                   | L                | Т        | P               | C                      |  |
|------------------|-------------------|----------------------|-----------------------------------------------------------------------------------------------|------------------|----------|-----------------|------------------------|--|
| YMA201           |                   | 01                   | LINEAR ALGEBRA                                                                                | 4                | 1        | 0               | 5                      |  |
| C                | P                 | A                    |                                                                                               |                  |          |                 |                        |  |
| 5                | 0                 | 0                    |                                                                                               | L                | Т        | P               | Н                      |  |
|                  |                   |                      |                                                                                               | 4                | 0        | 0               | 4                      |  |
| PRE              | REQU              | ISITE:               | Group theory and Ring theory                                                                  |                  |          |                 |                        |  |
| COU              | JRSE O            | UTCOM                | ES:                                                                                           |                  |          |                 |                        |  |
|                  | rse outco         |                      |                                                                                               | Doma             |          | Level           |                        |  |
|                  | Indepen           | dence an             |                                                                                               | Cogni            |          | Remen<br>Unders | tanding                |  |
| CO2              | 2: Defir          | ne and E             | <b>Explain</b> Dual Spaces- Inner Product Space- Modules.                                     | Cogni            | tive     | Remem<br>Unders | nbering<br>standing    |  |
| CO3              | Solve roots.      | the Alge             | bra of Linear Transformations to find characteristics                                         | Cogni            | tive     | Applyi          | ng                     |  |
| CO4              |                   |                      | xplain Canonical Forms, Triangular form, Nilpotent , Jordan Form and Rational Canonical form. | Cogni            | tive     | Remen<br>Unders |                        |  |
| CO5              |                   | itian, Un            | xplain Trace and Transpose, Determinants, itary and Normal Transformations, Real Quadratic    | Cognitive Rememl |          |                 | embering<br>erstanding |  |
| UNI              |                   | -                    |                                                                                               | <u> </u>         |          |                 | 15                     |  |
| Elen             | nentary           | Basic Co             | oncepts- Linear Independence and Bases.                                                       |                  |          |                 | i                      |  |
| UNI              | ΤΙΙ               |                      |                                                                                               |                  |          |                 | 15                     |  |
| Dual             | Spaces            | - Inner I            | Product Space- Modules.                                                                       |                  |          |                 |                        |  |
|                  | ТШ                |                      |                                                                                               |                  |          |                 | 15                     |  |
| The .            | Algebra           | of Line              | ar Transformations- Characteristics Roots- Matrices                                           |                  |          |                 |                        |  |
| UNI              |                   |                      |                                                                                               |                  |          |                 | 15                     |  |
| Cano<br>form     |                   | orms: Ti             | iangular form- Nilpotent Transformations- Jordan F                                            | Form - F         | Ration   | al Cano         | nical                  |  |
| UNI              |                   |                      |                                                                                               |                  |          |                 | 15                     |  |
|                  |                   | ranspose<br>tic form | – Determinants- Hermitian, Unitary and Normal Trs.                                            | ansforr          | natior   | 1S-             |                        |  |
| LI<br>60         | ECTUR             | E TU'                | ΓORIAL                                                                                        |                  |          | TO'             | ΓAL                    |  |
| <b>TEX</b> 1. He | TBOOK<br>erstein, | ζ<br>Ι.Ν.,"Το        | pics in Algebra", Willey Eastern 1975.                                                        |                  |          | i               |                        |  |
|                  |                   | •                    | (Section 4.1 & 4.2)  (Section 4.4 – 4.5) Unit III - Chapter 6 (Section 6)                     | 51 – 63          | 3)       |                 |                        |  |
|                  |                   | -                    |                                                                                               |                  |          | )               |                        |  |
| Ul               | 1111 I V -        | Chapter              | 6 (Section $6.4 - 6.7$ ) Unit V - Chapter 6 (Section $6.4 - 6.7$ )                            | 0.0              | – U. I I | .)              |                        |  |

- 1. John B. Fraleigh, "A First Course in Abstract Algebra", Narosa Publication, Third Edition, 2013.
- 2. P. M. Cohn, "Basic Algebra", Springer's Publications, Second Edition, 2003.

| COURSE CODE |                                                                                                                                               | ODE      | COURSE NAME                                                                                                       | L         | Т     | P          | С                     |  |
|-------------|-----------------------------------------------------------------------------------------------------------------------------------------------|----------|-------------------------------------------------------------------------------------------------------------------|-----------|-------|------------|-----------------------|--|
| YMA202      |                                                                                                                                               | 2        | ANALYSIS - II                                                                                                     | 4         | 1     | 0          | 5                     |  |
| С           | P                                                                                                                                             | A        |                                                                                                                   |           |       |            |                       |  |
| 5           | 0                                                                                                                                             | 0        |                                                                                                                   | L         | Т     | P          | H                     |  |
|             |                                                                                                                                               |          |                                                                                                                   | 4         | 1     | 0          | 5                     |  |
| PRE         | REQUI                                                                                                                                         | SITE:    | Basic concepts of convergence and uniform convergence                                                             | gence     |       |            | <u> </u>              |  |
| COU         | RSE OU                                                                                                                                        | JTCON    | IES:                                                                                                              |           |       |            |                       |  |
| Cour        | se outco                                                                                                                                      | mes:     |                                                                                                                   | Doma      | in    | Level      |                       |  |
| CO1         |                                                                                                                                               |          | Explain Existence, Properties of the Integral, and Differentiation.                                               | Cogni     | tive  | Remem      |                       |  |
| CO2         |                                                                                                                                               |          | Explain Uniform convergence and Continuity.                                                                       | Cogni     | tive  | Remem      | bering<br>tanding     |  |
| CO3         |                                                                                                                                               |          |                                                                                                                   |           |       |            | embering<br>rstanding |  |
| CO4         | CO4: Define and Explain Set functions, Construction of Lebesgue Measures, Measurable function, Simple functions in measure.  Cognitive Unders |          |                                                                                                                   |           |       |            | bering<br>tanding     |  |
| CO5         | : Defin                                                                                                                                       | e and l  | Explain Integration Comparison with the Riemann ration of Complex functions, Functions of class $\mathcal{J}^2$ . | Cogni     | tive  | Remem      |                       |  |
| UNI         |                                                                                                                                               |          | , , , , , , , , , , , , , , , , , , , ,                                                                           |           |       |            | 15                    |  |
| Defii       | nition ar                                                                                                                                     | nd Exist | ence of the Integral, Properties of the Integral, Integ                                                           | ration a  | nd Di | fferentia  | tion.                 |  |
| UNI         | ΓII                                                                                                                                           |          |                                                                                                                   |           |       |            | 15                    |  |
| Unifo       | orm Coi                                                                                                                                       | ivergen  | ce, Uniform convergence and Continuity.                                                                           |           |       |            |                       |  |
| UNI         | ΓIII                                                                                                                                          |          |                                                                                                                   |           |       |            | 15                    |  |
|             |                                                                                                                                               | vergen   | ce and Integration, Uniform convergence and Difference                                                            | entiation | ì.    |            | 1                     |  |
| UNI         | ΓIV                                                                                                                                           |          |                                                                                                                   |           |       |            | 15                    |  |
| ·····       |                                                                                                                                               | s, Const | ruction of Lebesgue Measures, Measurable function                                                                 | , Simple  | func  | tions in   |                       |  |
| meas        | sure.                                                                                                                                         |          | -                                                                                                                 |           |       |            |                       |  |
| UNI         |                                                                                                                                               |          |                                                                                                                   |           |       |            | 15                    |  |
|             |                                                                                                                                               | Compari  | son with the Riemann Integral, Integration of Comp                                                                | lex func  | tions | , Function | ons of                |  |
| class       |                                                                                                                                               | T TOT    | TODIAI                                                                                                            |           |       | тог        | ГАТ                   |  |
| 60          | ECTURI                                                                                                                                        | 15       | TORIAL                                                                                                            |           |       | 75         | ΓAL                   |  |
|             | ТВООК                                                                                                                                         | <b>.</b> |                                                                                                                   |           |       | 13         |                       |  |

1. Walter Rudin, "Principles of Mathematical Analysis", (3<sup>rd</sup> Edition), McGraw-Hill, 2016

Unit I - Chapter 6 (Pages: 120-135)

Unit II - Chapter 7 (Pages: 143-151)

Unit III - Chapter 7 (Pages: 151-154)

Unit IV - Chapter 11 (Pages: 300-314) Unit V - Chapter 5 (Section 314-325)

#### **REFERENCES:**

- 1. Shanti Narayan, "A course of Mathematical Analysis", S. Chand & Company Ltd New Delhi, 2005.
- 2. Apostol, T.M, "Mathematical Analysis", Narosa Book Distributors Pvt Ltd, 2<sup>nd</sup> Edition, New Delhi, 1996.
- 3. Malik, S.C, "Mathematical Analysis", Wiley Eastern Ltd. 2017.

| COURSE CODE |   | ODE | COURSE NAME           | L | Т | P | C |
|-------------|---|-----|-----------------------|---|---|---|---|
| YMA203      |   |     | DIFFERENTIAL GEOMETRY | 3 | 1 | 0 | 4 |
| С           | P | A   |                       |   |   |   |   |
| 4           | 0 | 0   |                       | L | Т | P | Н |
| <u> </u>    |   |     |                       | 3 | 1 | 0 | 4 |

# PREREQUISITE: Multivariable calculus and vector calculus

#### **COURSE OUTCOMES:**

| Course outcomes:                                                                                                                                       | Domain    | Level                     |
|--------------------------------------------------------------------------------------------------------------------------------------------------------|-----------|---------------------------|
| CO1: Define and Explain Arc length, tangent, normal and binormal                                                                                       | Cognitive | Remembering               |
| curvature and torsion, contact between curves and surfaces,                                                                                            |           | Understanding             |
| Tangent surface involutes and evolutes.                                                                                                                |           |                           |
| <b>CO2: Define and Explain</b> Surfaces of revolution, Helicoids, Families of curves and Isometric correspondence.                                     | Cognitive | Remembering Understanding |
| CO3: Define and Explain Normal property of geodesic, Geodesic parallels, Gaussian curvature and Conformal mapping.                                     | Cognitive | Remembering Understanding |
| CO4: Define and Explain Second fundamental form, Lines of curvature, Developables associated with curves on surfaces and Parallel surfaces.            | Cognitive | Remembering Understanding |
| CO5: Define and Explain Compact surfaces whose points are umbilics, Gaussian or mean curvature, Conjugate points on geodesics  Cognitive Remem Underst |           |                           |
| UNIT I                                                                                                                                                 |           | 12                        |

Definition of Space curves – Arc length – tangent – normal and binormal – curvature and torsion – contact between curves and surfaces – tangent surface – involutes and evolutes – intrinsic equations

| - Fundamental Existence Theorem for space curves - Helics.                                                                                                                                                                            |       |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|
| UNIT II                                                                                                                                                                                                                               | 12    |
| Definition of surface - Curves on a surface - Surfaces of revolution - Helicoids - Metric - Direction coefficients - Families of curves - Isometric correspondence - Intrinsic properties - Geodesics - Canonical geodesic equations. |       |
| UNIT III                                                                                                                                                                                                                              | 12    |
| Normal property of geodesic - Evistence theorems - Geodesic parallels - Geodesic curvature -                                                                                                                                          | Gance |

Normal property of geodesic - Existence theorems - Geodesic parallels - Geodesic curvature - Gauss Bonnet theorem - Gaussian curvature - Surfaces of constant curvature - Conformal mapping - Geodesic mapping.

UNIT IV 12

Second fundamental form - Principal curvatures- Lines of curvature — Developables - Developables associated with space curves - Developables associated with curves on surfaces- Minimal surfaces and ruled surfaces - Fundamental equations of Surface theory - Parallel surfaces.

UNIT V 12

Compact surfaces whose points are umbilics- Hilbert's lemma- Compact surfaces of constant Gaussian or mean curvature- Complete surfaces- Characterization of complete surfaces- Hilbert's theorem- Conjugate points on geodesics.

| LECTURE | TUTORIAL | TOTAL |
|---------|----------|-------|
| 45      | 15       | 60    |

#### **TEXTBOOK**

1. T. J. Wilmore, "An introduction to Differential Geometry", Oxford University Press, 1997.

- 1. Do Carmo, "Geometry of curves and surfaces", Academic Press, 2017.
- 2. D.Somasundaram, "Differential Geometry", Narosa Publ. House, Chennai, 2005.
- 3. J.A.Thorpe, "Elementary Topics in Differential Geometry", Springer Verlag, New York, 1979.

| COURSE CODE            |                                    | CODE                            | COURSE NAME                                                                                                                                                                                                                | L        | Т       | P                 | C               |
|------------------------|------------------------------------|---------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|---------|-------------------|-----------------|
| YMA204                 |                                    | )4                              | OPERATIONS RESEARCH                                                                                                                                                                                                        | 3        | 1       | 0                 | 4               |
| C                      | P                                  | A                               |                                                                                                                                                                                                                            |          |         |                   |                 |
| 4                      | 0                                  | 0                               |                                                                                                                                                                                                                            | L        | T       | P                 | Н               |
|                        |                                    |                                 |                                                                                                                                                                                                                            | 3        | 1       | 0                 | 4               |
| PRE                    | REQU                               | ISITE:                          | Nil                                                                                                                                                                                                                        |          |         |                   |                 |
| COU                    | JRSE O                             | UTCOM                           | IES:                                                                                                                                                                                                                       |          |         |                   |                 |
| Cour                   | rse outco                          | omes:                           |                                                                                                                                                                                                                            | Doma     |         | Level             |                 |
|                        |                                    |                                 | Explain Decision theory in detail.                                                                                                                                                                                         | Cogni    |         | Rement<br>Unders  | tanding         |
| CO2                    | 2: Expl                            | ain and                         | solve problems in PERT and CPM                                                                                                                                                                                             | Cogni    | tive    | Unders<br>Applyin | _               |
| CO3                    | _                                  | tory Co                         | ministic inventory control models and probabilistic ntrol Models and <b>solve</b> problems by using the                                                                                                                    | Cogni    | tive    | Unders<br>Applyin | _               |
| CO4                    |                                    |                                 | ntial Features of Queueing System, Classification of els and find solution of Queueing Models.                                                                                                                             | Cogni    | tive    | Unders<br>Remen   |                 |
| CO5                    | _                                  |                                 | acement and maintenance models and solve using these methods.                                                                                                                                                              | Cogni    | tive    | Unders<br>Applyii | _               |
|                        |                                    |                                 | THEORY                                                                                                                                                                                                                     |          |         |                   | 12              |
| Unde                   | er Unce                            | rtainty -                       | neory Approach - Types of Decision-Making Environeous Decision Making under Risk - Posterior Probabilitysis - Decision Making with Utilities.                                                                              |          |         |                   |                 |
| UNI                    |                                    |                                 | Γ MANAGEMENT : PERT AND CPM                                                                                                                                                                                                |          |         |                   | 12              |
| Netv                   | vork Co                            | mponer                          | etween PERT and CPM - Steps in PERT/CPM Tecl<br>its and Precedence Relationships - Critical Path Ana<br>oject time-cost Trade Off - Updating the Project - Re                                                              | alysis - | Prob    | ability i         |                 |
|                        |                                    |                                 | MINISTIC INVENTORY CONTROL MODELS                                                                                                                                                                                          |          |         |                   | 12              |
| Feati<br>short<br>Prob | ures of i<br>tage - D<br>abilistic | Inventor<br>etermin<br>Inventor | ory Control - Functional Classification - Advantage<br>ry System - Inventory Model building - Deterministic<br>istic Inventory with Shortages<br>ory Control Models:<br>abilistic Models without Setup cost - Single Perio | c Inver  | ntory ] | Models            | with no         |
|                        | <del>*</del>                       | UEUEI                           | NG THEORY                                                                                                                                                                                                                  |          |         |                   | 12              |
| Esse<br>Prob<br>Quei   | ntial F<br>abilistic<br>ueing M    | eatures<br>Distrib              | of Queueing System - Operating Characteristic<br>oution in Queueing Systems - Classification of Que<br>Probability Distribution of Arrivals and Departure                                                                  | ueing l  | Mode    | ls - Solı         | stem<br>ution o |
|                        |                                    |                                 | EMENT AND MAINTENANCE MODELS                                                                                                                                                                                               |          |         |                   | 12              |
|                        |                                    |                                 | of items - Replacement of Items Deteriorates with T                                                                                                                                                                        | ime - F  | Replac  | cement o          | of item         |
| 4 -                    | C '1                               | 1 , 1                           | other Depleasment Ducklams                                                                                                                                                                                                 |          |         |                   |                 |

that fail completely - other Replacement Problems.

| LECTURE | TUTORIAL | TOTAL |
|---------|----------|-------|
| 45      | 15       | 60    |

#### **TEXTBOOK**

1. J.K.Sharma, "Operations Research Theory and Applications", Third Edition, Macmillan India Ltd., 2007,

Unit I - Chapter-11 (Section 11.1 - 11.8)

Unit II - Chapter-13 (Section 13.1 - 13.9)

Unit III - Chapter-14 (Section 14.1 - 14.8); Chapter-15: (Section 15.1 - 15.4)

Unit IV - Chapter-16 (Section 16.1 - 16.9); Appendix 16. A (PP 774-781)

Unit V - Chapter-17 (Section 17.1 - 17.5)

#### **REFERENCES**

- 1.F.S. Hillier and J.Lieberman, "Introduction to Operations Research" (8th Edition), Tata McGraw Hill Publishing Company, New Delhi, 2006.
- 2. Beightler. C, D.Phillips, B. Wilde, "Foundations of Optimization" (2nd Edition) Prentice Hall Pvt Ltd., New York, 1979
- 3.Bazaraa, M.S; J.J.Jarvis, H.D.Sharall, "Linear Programming and Network flow", John Wiley and sons, New York, 1990.
- 4. Gross, D and C.M.Harris, "Fundamentals of Queueing Theory", (3<sup>rd</sup> Edition), Wiley and Sons, New York, 1998.
- 5. Hamdy A. Taha, "Operations Research" (sixth edition), Prentice Hall of India Private Limited, New Delhi. 2007

| COURSE CODE |   | CODE | COURSE NAME                | L | Т | P | C |
|-------------|---|------|----------------------------|---|---|---|---|
| YMAE205     |   | 05   | FUZZY SETS AND FUZZY LOGIC | 3 | 0 | 0 | 3 |
| С           | P | A    |                            |   |   |   |   |
| 3           | 0 | 0    |                            | L | Т | P | H |
|             | i |      |                            | 3 | 0 | 0 | 3 |

#### **PREREQUISITE:** Discrete Mathematics

#### **COURSE OUTCOMES:**

| Course outcomes:                                                                                                           | Domain    | Level                     |
|----------------------------------------------------------------------------------------------------------------------------|-----------|---------------------------|
| <b>CO1: Define and Explain</b> basic definitions of Crisp sets, the notion of fuzzy sets and basic concepts of fuzzy sets. | Cognitive | Remembering Understanding |
| CO2: Define and Explain operation on Fuzzy Sets.                                                                           | Cognitive | Remembering Understanding |

| CO3: Define and Explain Fuzzy Relations                                                               | Cognitive          | Remembering Understanding |  |  |  |  |  |
|-------------------------------------------------------------------------------------------------------|--------------------|---------------------------|--|--|--|--|--|
| CO4: Define and Explain Classical Logic.                                                              | Cognitive          | Remembering               |  |  |  |  |  |
| Understa                                                                                              |                    |                           |  |  |  |  |  |
| CO5: Define and Explain Fuzzy logic, fuzzy tautologies - Cognitive Remember                           |                    |                           |  |  |  |  |  |
| contradictions - equivalence and logical proofs.                                                      |                    | Understanding             |  |  |  |  |  |
| UNIT I Crisp Sets and Fuzzy Sets                                                                      | i                  | 9                         |  |  |  |  |  |
| Crisp sets basic definitions - the notion of fuzzy sets - basic concepts                              | of fuzzy sets.     | i                         |  |  |  |  |  |
| UNIT II Operation on Fuzzy Sets                                                                       |                    | 9                         |  |  |  |  |  |
| Fuzzy complement - fuzzy union - fuzzy intersection - combination a operations.                       | and general aggr   | egation                   |  |  |  |  |  |
| UNIT III Fuzzy Relations                                                                              |                    | 9                         |  |  |  |  |  |
| Crisp and fuzzy relations - binary relation - equivalence and similari - orderings.                   | ty relations - tol | erance relations          |  |  |  |  |  |
| UNIT IV Classical Logic                                                                               |                    | 9                         |  |  |  |  |  |
| Tautologies - contradictions - equivalence - exclusive OR and exclus                                  | ive NOR - logic    | al proofs.                |  |  |  |  |  |
| UNIT V Fuzzy Logic                                                                                    |                    | 9                         |  |  |  |  |  |
| Fuzzy logic - approximate reasoning - fuzzy tautologies - contradicti proofs.                         | ons - equivalenc   | e and logical             |  |  |  |  |  |
| LECTURE                                                                                               |                    | TOTAL                     |  |  |  |  |  |
| 45                                                                                                    |                    | 45                        |  |  |  |  |  |
| TEXTBOOKS                                                                                             |                    | 1 -0                      |  |  |  |  |  |
| 1. George J. Klir & Tina A. Folger, "Fuzzy Sets, Uncertainty, and In India Pvt. Ltd., New Delhi, 1988 | formation", Pren   | ntice Hall of             |  |  |  |  |  |
| 2. Timothy J. Ross, "Fuzzy Logic with Engineering Applications", 3 2010.                              | rd edition, McG    | raw-Hill. Inc,            |  |  |  |  |  |
| REFERENCES                                                                                            |                    |                           |  |  |  |  |  |
| 1.Zimmermann. H.J, "Fuzzy Set Theory and Its Applications", 4 <sup>th</sup>                           | edition, Spring    | er,                       |  |  |  |  |  |
| Netherlands, 2015.  2. Bart Kosko, "Neural Networks and Fuzzy Systems", Prentice-Hall                 | l International, 1 | 992.                      |  |  |  |  |  |

# **Semester III**

| COURSE CODE |        | •••••  | COURSE TITLE FIELD THEORY | L<br>3   | T<br>1 | P<br>0 | C |
|-------------|--------|--------|---------------------------|----------|--------|--------|---|
| YMA301      |        | /1     | FIELD THEORY              | 3        | 1      | U      | 4 |
| С           | P      | A      |                           |          |        |        |   |
| 4           | 0      | 0      |                           | L        | Т      | P      | Н |
|             | İ      | L      |                           | 3        | 1      | 0      | 4 |
| PRE         | EREQU  | ISITE: | Algebra                   | <u>I</u> | L      | L      |   |
| COU         | JRSE O | UTCON  | IES:                      |          |        |        |   |

| Course outcomes:                                                                                                       | Domain        | Level                                   |  |  |  |
|------------------------------------------------------------------------------------------------------------------------|---------------|-----------------------------------------|--|--|--|
| <b>CO1: Define and Explain</b> Extension fields – Finite Extension – Algebraic Extension - Transcendence of e.         | Cognitive     | Remembering Understanding               |  |  |  |
| CO2: Define and Explain Roots of Polynomials Remainder Theorem – Splitting field - More about roots.  Cognitive Unders |               |                                         |  |  |  |
| CO3: Define and Explain Elements of Galois Theory- Fixed field – Normal extension- Fundamental Theorem.                | Cognitive     | Remembering Understanding               |  |  |  |
| <b>CO4: Define and Explain</b> Solvability by radicals – Solvable group – Galois group over the rational.              | Cognitive     | Remembering Understanding               |  |  |  |
| CO5: Define and Explain Finite fields - Wedderburn's theorem on finite division rings – A Theorem of Frobenius.        | Cognitive     | Remembering Understanding               |  |  |  |
| UNIT I                                                                                                                 | <u>. i</u>    | 12                                      |  |  |  |
| Extension fields – Finite Extension – Algebraic Extension - Transcender                                                | nce of e.     | *************************************** |  |  |  |
| UNIT II  Roots of Polynomials Remainder Theorem – Splitting field - More about                                         | out roots.    | 12                                      |  |  |  |
| UNIT III                                                                                                               |               | 12                                      |  |  |  |
| Elements of Galois Theory- Fixed field – Normal extension- Fundamen                                                    | tal Theorem.  |                                         |  |  |  |
| UNIT IV                                                                                                                |               | 12                                      |  |  |  |
| Solvability by radicals – Solvable group – Galois group over the rational                                              | <b>1.</b>     | •                                       |  |  |  |
| UNIT V                                                                                                                 |               | 12                                      |  |  |  |
| Finite fields - Wedderburn's theorem on finite division rings – A Theorem of I                                         | Frobenius.    | · · · · · · · · · · · · · · · · · · ·   |  |  |  |
| 4 LECTURE TUTORIAL                                                                                                     |               | TOTAL                                   |  |  |  |
| 45                                                                                                                     |               | 60                                      |  |  |  |
| 1. N. Herstein,"Topics in Algebra", Willey Eastern, 1975.                                                              |               |                                         |  |  |  |
| REFERENCES                                                                                                             |               |                                         |  |  |  |
| 1. John B. Fraleigh,"A First Course in Abstract Algebra", Narosa Public                                                | cation, Third | Edition, 2013                           |  |  |  |
| 2. P. M. Cohn,"Basic Algebra", Springers Publications, Second Edition                                                  | , 2003.       |                                         |  |  |  |

| COU             | JRSE (    | CODE           | COURSE NAME                                                                   | $\mathbf{L}$ | T        | P               | C        |
|-----------------|-----------|----------------|-------------------------------------------------------------------------------|--------------|----------|-----------------|----------|
| YMA302          |           | 2              | TOPOLOGY                                                                      | 4            | 1        | 0               | 5        |
| С               | P         | A              |                                                                               |              |          |                 |          |
| 5               | 0         | 0              |                                                                               | L            | Т        | P               | H        |
|                 |           |                |                                                                               | 4            | 1        | 0               | 5        |
| PRE             | REQU      | ISITE:         | Analysis                                                                      |              | <u> </u> |                 | <u> </u> |
| COU             | RSE O     | JTCOM          | TES:                                                                          |              |          |                 |          |
| Cour            | se outco  | mes:           |                                                                               | Doma         | in       | Level           |          |
| CO <sub>1</sub> | : Defin   | e and          | Explain Topological Spaces                                                    | Cogni        | tive     | Remem           |          |
| CO2             | . D.C.    |                | Francis Continuous Frantisms                                                  | Cooni        | +:       | Underst         | <u> </u> |
| COZ             | : Denn    | ie and 1       | Explain Continuous Functions                                                  | Cogni        | uve      | Remem<br>Unders | tanding  |
| CO3             | : Defin   | e and <b>E</b> | Explain Connectedness                                                         | Cogni        | tive     | Remem           |          |
| CO4             | : Defin   | e and F        | Explain Compactness                                                           | Cogni        | tive     | Remem           | _        |
| CO5             | : Defin   | e and l        | Explain Countability and Separation Axiom                                     | Cogni        | tive     | Remem           |          |
| UNIT            | TI Top    | ologic         | al Spaces                                                                     | •            |          |                 | 15       |
| Topo            | logical   | spaces         | - Basis for a topology - The order topology - The p                           | product to   | polog    | y               |          |
| on $X$          | x Y - T   | he subs        | space topology.                                                               |              |          |                 |          |
| UNIT            | II Co     | ntinuoı        | is Functions                                                                  |              |          |                 | 15       |
| Close           | ed sets a | and limi       | t points-Continuous functions - the product topolo                            | gy - The     | metric   | ;               |          |
| topo            | logy '    | The me         | tric topology (continued) - Uniform limit theorem.                            |              |          |                 |          |
| UNIT            | T III (   | Connect        | tedness                                                                       |              |          |                 | 15       |
| Conn            | ected s   | paces -        | connected subspaces of the Real line - Component                              | s and loca   | ıl con   | nectedn         | ess.     |
| UNIT            | ΓIV C     | ompact         | tness                                                                         |              |          |                 | 15       |
|                 |           |                | compact subspaces of the Real line - Limit                                    | Point C      | ompa     | ctness -        | Local    |
| Com             | pactnes   | S.             |                                                                               |              |          |                 |          |
| UNIT            | ΓV Co     | untabi         | lity and Separation Axiom                                                     |              |          |                 | 15       |
|                 |           |                | xioms - The separation Axioms - Normal spaces                                 | - The Ur     | ysohr    | Lemm            | a - The  |
| Urys            | ohn me    | trizatio       | n Theorem - The Tietz extension theorem.                                      |              |          |                 |          |
| LF              | ECTURI    | E <b>T</b> U   | TORIAL                                                                        |              |          | TO              | ΓAL      |
| 45              |           | 15             |                                                                               |              |          | 60              |          |
|                 | TBOOK     |                | (ID 1 N (0 1 D 11)                                                            | T. 1         |          | r 1• =          |          |
|                 | ew Dell   | i, 2014        | res, "Topology", (2nd Edition) PHI Learning Pvt<br>apter 2: Sections 12 to 17 | . Ltd., (T   | hird 1   | Indian I        | Reprint) |

Unit II - Chapter 2: Sections 18 to 21 (Omit Section 22)

Unit III - Chapter 3: Sections 23 to 25

Unit IV - Chapter 3: Sections 26 to 29

Unit V - Chapter 4: Sections 30 to 35

- 1. J. Dugundji, "Topology", Prentice Hall of India, New Delhi, 1975.
- 2. George F.Sinmons, "Introduction to Topology and Modern Analysis", McGraw Hill Book Co., 1963.
- 3. J.L. Kelly, "General Topology", Van Nostrand, Reinhold Co., New York. 1995
- 4. L.Steen and J.Subhash, "Counter Examples in Topology", Holt, Rinehart and Winston, New York, 1970.
- 5. S.Willard, "General Topology", Addison Wesley, Mas.1970.

| COURSE CODE                                                                                         |                | CODE    | COURSE NAME                                             | L               | T                           | P     | C        |
|-----------------------------------------------------------------------------------------------------|----------------|---------|---------------------------------------------------------|-----------------|-----------------------------|-------|----------|
| YMA303                                                                                              |                | )3      | MEASURE THEORY                                          | 3               | 1                           | 0     | 4        |
| С                                                                                                   | P              | A       |                                                         |                 |                             |       |          |
| 4                                                                                                   | 0              | 0       |                                                         | L               | Т                           | P     | Н        |
|                                                                                                     |                |         |                                                         | 3               | 1                           | 0     | 4        |
|                                                                                                     | REQU<br>IRSE O |         | Analysis  TES:                                          |                 |                             |       | <u> </u> |
|                                                                                                     | se outco       |         |                                                         | Doma            | in                          | Level |          |
| CO1: Define and Explain Measure Spaces – Measurable functions – Integration                         |                |         | Cognitive                                               |                 | Remembering<br>Understandin |       |          |
| CO2: Define and Explain General Convergence Theorems – Signed measures – The Radon Nikodym Theorem. |                |         |                                                         | Remem<br>Unders | _                           |       |          |
| 002                                                                                                 | . Dofin        | a and I | Explain The L <sup>p</sup> – spaces – Outer measure and | Cogni           | fixa                        | Remem | harina   |

| CO2: Define and Explain General Convergence Theorems – Signed measures – The Radon Nikodym Theorem.                            | Cognitive | Remembering Understanding               |
|--------------------------------------------------------------------------------------------------------------------------------|-----------|-----------------------------------------|
| <b>CO3: Define and Explain</b> The L <sup>p</sup> – spaces – Outer measure and measurability- The Extension Theorem.           | Cognitive | Remembering Understanding               |
| <b>CO4: Define and Explain</b> The Lebesgue-Stieltjes integral – Product measures – Integral operators.                        | Cognitive | Remembering Understanding               |
| <b>CO5: Define and Explain</b> Inner measure – Extension by sets of measure zero- Caratheodory outer measure Hausdorff measure | Cognitive | Remembering Understanding               |
| UNIT I                                                                                                                         |           | 12                                      |
| Measure Spaces – Measurable functions – Integration.                                                                           |           |                                         |
| UNIT II                                                                                                                        |           | 12                                      |
| General Convergence Theorems – Signed measures – The Radon Nikody                                                              | m Theorem | 1.                                      |
| UNIT III                                                                                                                       |           | 12                                      |
| The L <sup>p</sup> – spaces – Outer measure and measurability- The Extension Theo                                              | orem.     | *************************************** |

| UNIT IV                                                                               | 12           |
|---------------------------------------------------------------------------------------|--------------|
| The Lebesgue-Stieltjes integral – Product measures – Integral operate                 | ors.         |
| UNIT V                                                                                | 12           |
|                                                                                       | 4            |
| Inner measure – Extension by sets of measure zero- Caratheodory or                    | uter measure |
| Inner measure – Extension by sets of measure zero- Caratheodory of Hausdorff measure. | uter measure |
|                                                                                       | TOTAL        |
| Hausdorff measure.                                                                    | Ψ            |
| Hausdorff measure.  LECTURE TUTORIAL                                                  | TOTAL        |

1.H.L.Royden, Real Analysis, 3<sup>rd</sup> Edition, Standford University, Prentice – Hall of India private Limited, New Delhi. 2002.

(Chapter 11 - Section 1 to 7, Chapter 12 - Section 1 to 9).

### **REFERENCES**

- 1.P.R. Halmos, "Measure Theory", Graduate Text in Mathematics, Springer-Verlag, 1979.
- 2.Inder K. Rana, "An Introduction to Measure and Integration",  $(2^{nd} \text{ ed.})$ , Narosa Publishing House, New Delhi, 2004.

| COURSE CODE |   | CODE | COURSE NAME             | COURSE NAME L |   | COURSE NAME |   | Т | P | C |
|-------------|---|------|-------------------------|---------------|---|-------------|---|---|---|---|
| YMA304      |   | )4   | MATHEMATICAL STATISTICS | 3             | 1 | 0           | 4 |   |   |   |
| C           | P | A    |                         |               |   |             |   |   |   |   |
| 4           | 0 | 0    |                         | L             | Т | P           | Н |   |   |   |
|             |   |      |                         | 3             | 1 | 0           | 4 |   |   |   |

PREREQUISITE: Nil

### **COURSE OUTCOMES:**

| Course outcomes:                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | Domain    | Level                     |  |  |  |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------|---------------------------|--|--|--|
| CO1: Define and Explain Estimation Theory.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | Cognitive | Remembering Understanding |  |  |  |
| <b>CO2:</b> Explain and solve Tests based on normal, t and f distributions for testing of means, variance and proportions – Analysis of r × c tables – Goodness of fit                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Cognitive | Understanding  Applying   |  |  |  |
| CO3: Explain and solve Correlation And Regression.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | Cognitive | Understanding<br>Applying |  |  |  |
| CO4: Explain and solve Design of Experiments                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | Cognitive | Understanding<br>Applying |  |  |  |
| 200 2 production of the control of t |           | Understanding Applying    |  |  |  |
| UNIT I Estimation Theory                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |           |                           |  |  |  |

Estimators: Un biasedness, Consistency, Efficiency and Sufficiency – Maximum likelihood

| 12 |
|----|
|    |
| 12 |
|    |

Multiple and Partial correlation – Method of least squares – Plane of Regression – Properties of residuals – Coefficient of multiple correlation – Coefficient of partial correlation – Multiple correlation with total and partial correlation – Regression and Partial correlations in terms of lower order co-efficient.

## **UNIT IV Design of Experiments**

12

Analysis of variance – One way and two way classifications – Completely randomized design – Randomized block design – Latin square design.

## **UNIT V Statistical Quality Control**

12

Analysis of variance: Control charts for measurements (X and R charts) – control charts for attributes (p, c and np charts) – Tolerance limits – Acceptance sampling, Introduction to SPSS.

| LECTURE | TUTORIAL | TOTAL |
|---------|----------|-------|
| 45      | 15       | 60    |

#### **TEXTBOOK**

1. Gupta. S.C., and Kapoor. V.K., "Fundamentals of Mathematical Statistics", Sultan Chand and sons, Thirteenth Edition, 2014.

#### REFERENCES

- 1. J.E. Freund, "Mathematical Statistical", 5<sup>th</sup> Edition, Prentice Hall of India, 2001.
- 2. Jay L. Devore, "Probability and Statistics for Engineering and the Sciences",5<sup>th</sup> Edition, Thomas and Duxbury, Singapore, 2002.

| COURSE CODE |                | CODE | COURSE NAME       | L | Т | P | C |
|-------------|----------------|------|-------------------|---|---|---|---|
| , Y         | YMA3E02  C P A |      | NUMERICAL METHODS | 3 | 0 | 0 | 3 |
| С           | P              | A    |                   |   |   |   |   |
| 3           | 0              | 0    |                   | L | Т | P | H |
|             | ·              |      |                   | 3 | 0 | 0 | 3 |

**PREREQUISITE:** Algebra

| COURSE OUTCOMES:                                                                                            |                |             |          |
|-------------------------------------------------------------------------------------------------------------|----------------|-------------|----------|
| Course outcomes:                                                                                            | Domain         | Level       |          |
| <b>CO1:</b> Find the solution by using Bisection method-Newton-Raphson                                      | Cognitive      | Remembe     | ering    |
| Method-Curve fitting straight line and parabola.                                                            |                |             |          |
| CO2: Solve Simultaneous Linear Equations.                                                                   | Cognitive      | Remembe     |          |
|                                                                                                             |                | Understa    | nding    |
| <b>CO3: Find</b> the value of $y = f(x)$ using interpolation formula.                                       | Cognitive      | Remembe     | ring     |
| $\mathbf{Cos. Time the value of } \mathbf{y} = \mathbf{i}(\mathbf{x}) \text{ using interpolation formula.}$ | Cogmitive      | Understar   | _        |
| <b>CO4: Find</b> the first and second derivative of $f(x)$ and to find the value                            | Cognitive      | Remembe     |          |
| of integrals using numerical methods.                                                                       |                | Understar   | _        |
| CO5: Solve ordinary differential equations by using various methods.                                        | Cognitive      | Remembe     | ering    |
| , , , , , , , , , , , , , , , , , , , ,                                                                     | _              | Understar   | nding    |
| UNIT I                                                                                                      |                |             | 9        |
| Solution of Numerical Algebraic Equations & Curve fitting Bisection                                         | on method-N    | Iewton-Raj  | phson    |
| method-Curve fitting straight line and parabola.                                                            |                |             |          |
| UNIT II                                                                                                     |                |             | 9        |
| Solution of Simultaneous Linear Equations-Gauss-Elimination                                                 | method-Me      | thod of     | •        |
| factorization-Gauss Jacobi and Gauss-Seidel methods                                                         |                |             |          |
| UNIT III                                                                                                    |                |             | 9        |
| Interpolation - Gregory-Newton forward and backward interpolation f                                         | formulae Ste   | rling's for | mula-    |
| Lagrange's formula.                                                                                         |                |             |          |
| UNIT IV                                                                                                     |                |             | 9        |
| Numerical Differentiation and Integration, Numerical differentiation,                                       | Trapezoidal    | rule-Simp   | son's    |
| one-third rule —Simpson's three-eighth rule.                                                                |                |             |          |
| UNIT V                                                                                                      |                |             | 9        |
| Numerical Solution of Ordinary Differential Equations, Euler's method                                       | l – fourth ord | ler Runge-  | Kutta    |
| method-Milne's predictor corrector method.                                                                  |                |             |          |
| LECTURE                                                                                                     |                | TOTA        | <b>L</b> |
| 45                                                                                                          |                | 45          |          |
| TEXTBOOK                                                                                                    |                |             |          |
| 1. Sastry.S.S, "Introductory Methods of Numerical Analysis", Pren                                           | tice Hall of I | ndia, 2000  | ).       |
| REFERENCES                                                                                                  |                |             |          |
| 1. Gerald, Curtis and Wheatley, Patrick.O,"Applied Numerical                                                | Analysis",     | (Fifth Ed   | lition)  |
| Addison-Wesley, 1989.                                                                                       | • •            | `           | ,        |
| 2 Kandasamu D. Thilalrayathu K. Cunayathu K. Nyumani ad Matha                                               | la C Chand (   | C. C. I.1   | NT       |

2. Kandasamy.P, Thilakavathy.K, Gunavathy.K-Numerical Methods, S.Chand & Co. Ltd, New Delhi, Reprint 2001.

| COUR     | SE CO         | )DE                        | COURSE NAME                                                                                                      | L        | Т       | P         | С      |
|----------|---------------|----------------------------|------------------------------------------------------------------------------------------------------------------|----------|---------|-----------|--------|
| YN       | <b>IA401</b>  |                            | COMPLEX ANALYSIS                                                                                                 | 4        | 1       | 0         | 5      |
|          |               |                            |                                                                                                                  |          |         |           |        |
| C        | P             | A                          |                                                                                                                  |          |         |           |        |
| 5        | 0             | 0                          |                                                                                                                  | L        | Т       | Р         | Н      |
|          |               |                            |                                                                                                                  | 4        | 1       | 0         | 5      |
| PRERI    | EQUIS         | SITE:                      | Analysis                                                                                                         |          |         |           |        |
| COURS    | SE OU         | ГСОМ                       | TES:                                                                                                             |          |         |           |        |
| Course   |               |                            |                                                                                                                  | Doma     | in      | Level     |        |
|          |               |                            | Explain Line Integrals- Rectifiable arc – Line                                                                   | Cogni    |         | Remem     | bering |
|          | integra       | ıls as f                   | functions of arc- Cauchy's Theorem for rectangle-                                                                | 8        |         | Underst   | _      |
|          |               | <del>-</del>               | Explain Integral Formula – Higher derivatives –                                                                  | Cogni    | tive    | Remem     | bering |
|          |               |                            | ngularities – Taylor's theorem – Zeros and Poles –                                                               |          |         | Underst   | anding |
| T        | he Loc        | cal Ma                     | pping – The Maximum Principle.                                                                                   |          |         |           |        |
| CO3: I   | <b>Define</b> | and E                      | xplain The General Statement of Cauchy's                                                                         | Cogni    | tive    | Remem     |        |
| T        | 'heorer       | n – Pr                     | oof of Cauchy's Theorem – Locally Exact                                                                          |          |         | Underst   | anding |
|          |               |                            | - Multiply Connected Regions.                                                                                    |          |         |           |        |
|          |               |                            | <b>xplain</b> The Residue Theorem – The Argument                                                                 | Cogni    | tive    | Remem     | _      |
|          |               |                            | aluation of Definite Integrals – The Mean – value                                                                |          |         | Underst   | anding |
|          |               |                            | sson's formula- Schwarz's Theorem – The                                                                          |          |         |           |        |
|          | Reflecti      |                            |                                                                                                                  |          |         |           |        |
|          |               |                            | xplain Weierstrass's Theorem – The Taylor Series                                                                 | Cogni    | tive    | Remem     |        |
|          |               |                            | Series – Partial Fractions- Jensen's Formula –                                                                   |          |         | Underst   | anding |
|          | ladama        | ard's I                    | heorem                                                                                                           |          |         |           |        |
| UNIT I   | 1             | D (                        |                                                                                                                  | , 101    |         | C         | 15     |
|          | _             |                            | ifiable arc – Line integrals as functions of arc- Cauch                                                          | ny's The | eoren   | i for rec | angle- |
| Cauchy   |               | orem 1                     | or disc.                                                                                                         |          |         |           | 1.5    |
| UNIT I   |               |                            |                                                                                                                  |          | •       |           | 15     |
|          |               | -                          | nt - Integral Formula – Higher derivatives – Remo                                                                |          | _       |           | -      |
|          |               | em – 2                     | Zeros and Poles – The Local Mapping – The Maximo                                                                 | um Prin  | icipie  | •         | 15     |
| UNIT I   |               |                            | Simple Connectivity Hemelegy The Cone                                                                            | 1 C+-4   |         | t of Co   | 15     |
|          |               | •                          | <ul> <li>Simple Connectivity – Homology – The Gene<br/>of Cauchy's Theorem – Locally Exact Differenti</li> </ul> |          |         |           | •      |
| Regions  |               | 1001 (                     | of Cauchy's Theorem – Locary Exact Differenti                                                                    | .ais — 1 | viuitij | ory Con   | necteu |
| UNIT I   |               |                            |                                                                                                                  |          |         |           | 15     |
|          |               | Cheore                     | m – The Argument Principle – Evaluation of Defin                                                                 | ite Inte | orale   | _ The N   |        |
|          |               |                            | sson's formula- Schwarz's Theorem – The Reflection                                                               |          |         | THE I     | 20011  |
| UNIT V   |               | 1 01                       |                                                                                                                  |          | -r -c · |           | 15     |
|          |               | Theo                       | rem – The Taylor Series – The Laurent Series –                                                                   | Partial  | Fract   | ions- Je  |        |
|          |               |                            | d's Theorem.                                                                                                     |          |         |           |        |
|          | TURE          | ······ <del>?</del> ······ | TORIAL                                                                                                           |          |         | TO        | ΓAL    |
| 60       |               | 15                         |                                                                                                                  |          |         | 75        |        |
| TEXTB    |               |                            |                                                                                                                  |          |         |           |        |
| 1.Lars \ | V.Ahlf        | ors, "                     | Complex Analysis", 3 <sup>rd</sup> Edition McGraw Hill Educa                                                     | tion (In | dia) F  | rivate    |        |

### Ltd.2013.

Chapter 4 - Section 1.1 to 1.5, Section 2.1 to 2.3, Section 3.1 to 3.4, Section 4.1 to 4.7, Section 5.1 to 5.3, Section 6.1 to 6.5.

Chapter 5 - Section 1.1 to 1.3, Section 2.1, Section 3.1 & 3.2.

### **REFERENCES:**

1. S. Poonusamy, "Complex Analysis", Alpha Science International Ltd; 2<sup>nd</sup> Revised edition, 2005.

| CO | COURSE CODE COURSE NAME                                                                         |   | L | Т   | P | C |   |
|----|-------------------------------------------------------------------------------------------------|---|---|-----|---|---|---|
|    | OURSE CODE COURSE NAME IL YMA402 FUNCTIONAL ANALYSIS 4  P A I I I I I I I I I I I I I I I I I I |   | 4 | 4 1 | 0 | 5 |   |
| C  | P                                                                                               | A |   |     |   |   |   |
| 5  | 0                                                                                               | 0 |   | L   | Т | P | Н |
|    | I                                                                                               |   |   | 4   | 1 | 0 | 5 |

# **PREREQUISITE:** Analysis

## **COURSE OUTCOMES:**

| Course outcomes:                                            | Domain    | Level         |
|-------------------------------------------------------------|-----------|---------------|
| CO1: Define and Explain Normed Spaces – Continued of Linear | Cognitive | Remembering   |
| Maps – Hahn – Banach Theorems.                              |           | Understanding |
| CO2: Define and Explain Banach Spaces – Uniform Boundedness | Cognitive | Remembering   |
| Principle – Closed Graph and Open Mapping Theorems.         |           |               |

|                                                                                                                                                                                                     |                                       | Understa            | nding      |  |  |  |  |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------|---------------------|------------|--|--|--|--|
| <b>CO3: Define and Explain</b> Bounded Inverse Theorem – Spectrum of a Bounded Operator.                                                                                                            | rum of a Cognitive Rememb<br>Understa |                     |            |  |  |  |  |
| CO4: Define and Explain Inner Product Spaces – Orthonormal Sets – Projection and Riesz Representation Theorems.  Cognitive Rememburgers – Understa                                                  |                                       |                     |            |  |  |  |  |
| CO5: Define and Explain Bounded Operators and adjoint, Normal, Unitary and Self-adjoint Operators.                                                                                                  | Cognitive                             | Remembe<br>Understa |            |  |  |  |  |
| UNIT I                                                                                                                                                                                              |                                       |                     | 15         |  |  |  |  |
| Normed Spaces – Continued of Linear Maps – Hahn – Banach Theorem                                                                                                                                    | ns.                                   |                     |            |  |  |  |  |
| UNIT II                                                                                                                                                                                             |                                       |                     | 15         |  |  |  |  |
| Banach Spaces – Uniform Boundedness Principle – Closed Graph Theorems.                                                                                                                              | and Open                              | Mapping             |            |  |  |  |  |
| UNIT III                                                                                                                                                                                            |                                       |                     | 15         |  |  |  |  |
| Bounded Inverse Theorem – Spectrum of a Bounded Operator.                                                                                                                                           |                                       |                     |            |  |  |  |  |
| UNIT IV                                                                                                                                                                                             |                                       |                     | 15         |  |  |  |  |
| Inner Product Spaces – Orthonormal Sets – Projection and Riesz Repres                                                                                                                               | sentation The                         | orems.              |            |  |  |  |  |
| UNIT V                                                                                                                                                                                              |                                       |                     | 15         |  |  |  |  |
| Bounded Operators and adjoint, Normal, Unitary and Self-adjoint Ope                                                                                                                                 | rators.                               |                     | .1         |  |  |  |  |
| LECTURE TUTORIAL                                                                                                                                                                                    |                                       | TOTA                | <b>\</b> L |  |  |  |  |
| 60 15                                                                                                                                                                                               |                                       | 75                  |            |  |  |  |  |
| <b>TEXTBOOK</b> 1.Balmohan V Limaye, "Functional Analysis", 3 <sup>rd</sup> Edition, New Age In Publishers, New Delhi, 2017.                                                                        | ternational (F                        | P) Limited          |            |  |  |  |  |
| REFERENCES                                                                                                                                                                                          |                                       |                     |            |  |  |  |  |
| <ol> <li>G.F. Simmons, "Introduction to Topology and Modern<br/>International Book Company, New York, 1963.</li> <li>W. Rudin, "Functional Analysis", Tata McGraw-Hill Publish<br/>1973.</li> </ol> | •                                     |                     |            |  |  |  |  |
| <ol> <li>E. Kreyszig, "Introductory Functional Analysis with Application New York, 1978.</li> <li>H. C. Goffman and G.Fedrick, "First Course in Functional Analysis"</li> </ol>                     |                                       | •                   |            |  |  |  |  |

 H. C. Goffman and G.Fedrick, "First Course in Functional Analysis", Prentice Hall of India, New Delhi, 1987.

| COURSE CODE<br>YMA403 |       | ODE | COURSE NAME          | L | T | P | С |
|-----------------------|-------|-----|----------------------|---|---|---|---|
| 7                     | YMA40 | 3   | STOCHASTIC PROCESSES | 3 | 1 | 0 | 4 |
| С                     | P     | A   |                      |   |   |   |   |
| 4                     | 0     | 0   |                      | L | Т | P | Н |

|                                                                                                                                                                                                                                      | 3        |       | 1  | 0               | 4        | 4             |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|-------|----|-----------------|----------|---------------|
| PREREQUISITE: Probability and Statistics                                                                                                                                                                                             | <u> </u> |       |    |                 | <u> </u> |               |
| COURSE OUTCOMES:                                                                                                                                                                                                                     |          |       |    |                 |          |               |
| Course outcomes:                                                                                                                                                                                                                     | Doma     | ain   |    | Level           |          |               |
| CO1: Define and Explain Specification of Stochastic processes,<br>Stationary processes, Markov Chains with examples                                                                                                                  | Cogn     |       |    | Remen<br>Unders | standi   | ng            |
| CO2: Define and Explain Classification of states and chains.                                                                                                                                                                         | Cogn     | itive |    | Remen<br>Under  |          | $\mathcal{C}$ |
| CO3: Define and Explain Markov processes with Discrete state space.                                                                                                                                                                  | Cogn     | itive |    | Remen<br>Unders |          |               |
| CO4: Define and Explain Queuing system                                                                                                                                                                                               | Cogn     | itive |    | Remen<br>Unders | standi   | ng            |
| CO5: Define and Explain Auto-correlation functions, cross-                                                                                                                                                                           | Cogn     | itive |    | Remen           |          |               |
| correlation functions and their properties  UNIT I                                                                                                                                                                                   |          |       |    | Unders          |          | ng<br>2       |
| Stochastic Processes: Some notions, Specification of Stochastic proce<br>Markov Chains – Definitions and examples – Higher Transition proba<br>Independent Bernoulli trails – Sequence of chain – Dependent trains.                  |          |       |    |                 |          |               |
| UNIT II                                                                                                                                                                                                                              |          |       |    |                 | 1        | 2             |
| Markov chains: Classification of states and chains – determination probabilities – stability of a Markov system – Reducible chains – continuous state space.                                                                         |          | _     |    |                 | th       |               |
| UNIT III                                                                                                                                                                                                                             | 41 :     |       |    |                 | <u>i</u> | 2             |
| Markov processes with Discrete state space: Poisson processes and process and related distribution – Generalization of Poisson process-Markov processes with discrete state space (continuous time Markov Charles)                   | Birth    |       |    |                 |          |               |
| UNIT IV                                                                                                                                                                                                                              |          |       |    |                 | 1        | 2             |
| Stochastic processes in Queuing – Queuing system – General concepts – Steady state behaviour – transient behaviour of M/M/1 Model- Bi queuing theory: Muti-channel models.                                                           | _        |       | _  |                 |          |               |
| UNIT V  Auto-correlation functions, cross-correlation functions - properties, pow spectral density — Properties - Wiener-Khinchine relation, linear time transfer function — auto-correlation and cross-correlation functions of inp | invar    | iant  | sy | stem -          | - Cro    |               |
| LECTURE TUTORIAL                                                                                                                                                                                                                     |          |       |    | ТО              | TAL      |               |
| 45 15                                                                                                                                                                                                                                |          |       |    | 60              |          |               |
| <ul> <li>TEXTBOOK</li> <li>1.J. Medhi, "Stochastic Processes", New Age International (P) Limited, I edition. 2013</li> <li>2. T. Veerarajan, "Random Processes", Tata McGraw Hill Publishing Co Delhi, 2008</li> </ul>               |          |       |    |                 | cond     |               |
| REFERENCES:                                                                                                                                                                                                                          |          |       |    |                 |          |               |

- 1. Peebles, P.Z., "Probability, Random Variables and Random Signal Principles", Tata McGraw Hill, 4<sup>th</sup> edition, New Delhi, (2002).
- 2. Srinivasan and Metha, Stochastic Processes,
- 3. Miller, S.L. and Childers, D.G., "Probability and Random Processes with Applications to Signal Processing and Communications", Academic Press, (2004).
- 4. R. Nelson, Probability, "Stochastic Processes, and Queuing Theory: The Mathematics of Computer Performance Modeling", Springer-Verlag, New York, 1995.